

~~Algebra~~ 15. Feb 11, 4c

$$\text{Algebra} \left(\frac{\delta f(u)}{\delta u} = \frac{\partial}{\partial u} \sum_{i=0}^n b_i \beta_i^n(u) \right)$$

$$= \sum_{i=0}^n b_i \cdot u \left(\beta_{i-1}^{n-1}(u) - \beta_i^{n-1}(u) \right)$$

$$= u \cdot \left(\sum_{i=0}^n b_i \beta_{i-1}^{n-1}(u) - \sum_{i=0}^n b_i \beta_i^{n-1}(u) \right)$$

$$= u \left(\sum_{i=1}^n b_i \beta_{i-1}^{n-1}(u) - \sum_{i=0}^{n-1} b_i \beta_i^{n-1}(u) \right)$$

$$= u \left(\sum_{i=0}^{n-1} b_{i+1} \beta_i^{n-1}(u) - \sum_{i=0}^{n-1} b_i \beta_i^{n-1}(u) \right)$$

$$= \sum_{i=0}^{n-1} \underbrace{(n(b_{i+1} - b_i))}_{=: c_i} \beta_i^{n-1}(u)$$